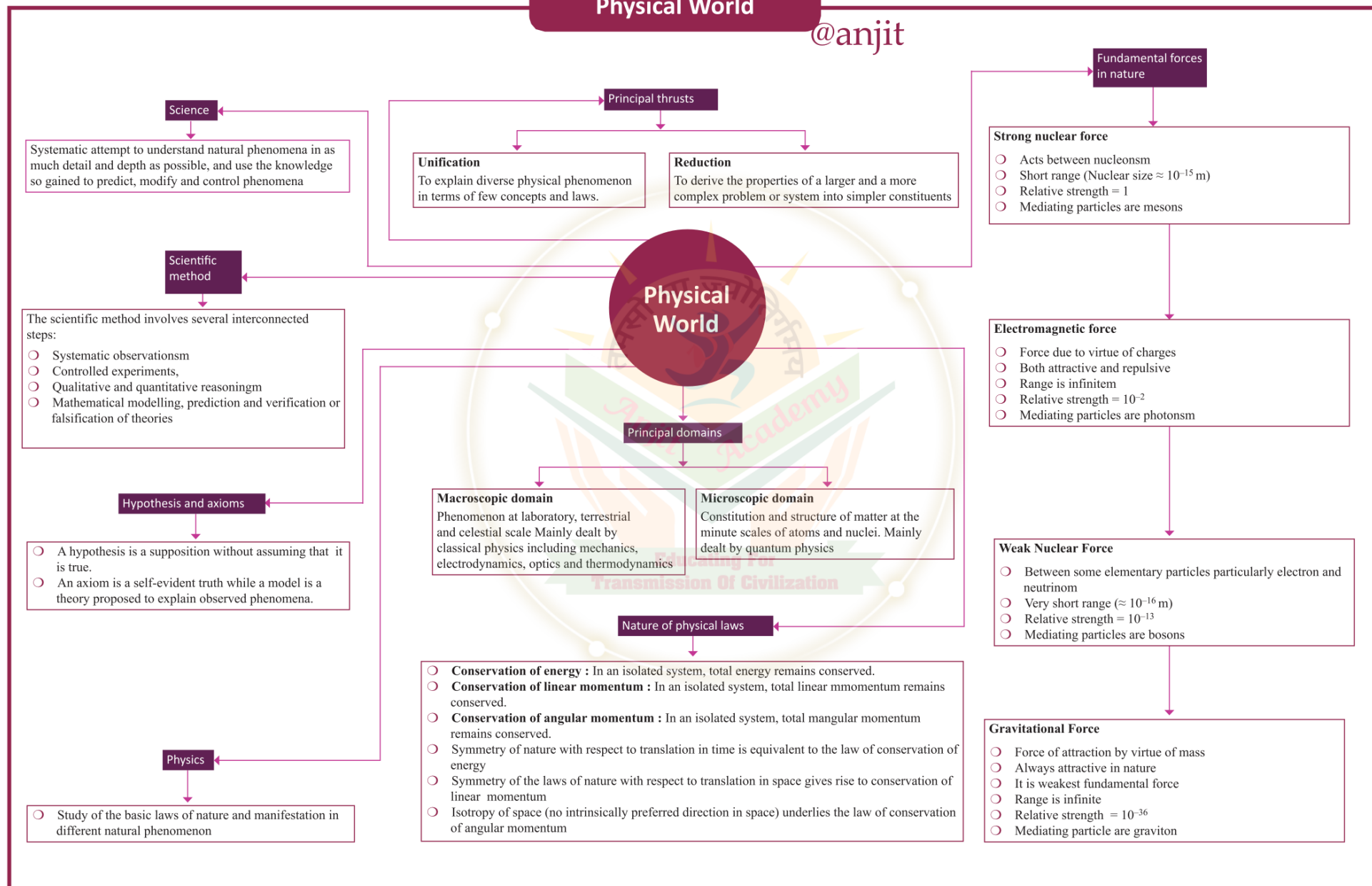


Physical World

@anjit



Units

Measurement of any physical quantity involves comparison with certain basic arbitrarily chosen internationally accepted reference called units.

Classification

Fundamental units

Independent of each other

Derived units

Expressed as combination of fundamental units

- A complete set of these units, both the base units and derived units is known as system of units.
- Old system of units: CGS, FPS and MKS system.
- In CGS fundamental units are centimeter, gram and second.
- In FPS fundamental units are foot, pound and second.
- In MKS fundamental units are meter, kilogram and second.

Measurement of length

- Large distance is measured by parallax method.
- Parallax angle = $\frac{\text{Basis}}{\text{Distance}}$
- $1^\circ = 1.745 \times 10^{-2}$ rad
- $1'' = 4.85 \times 10^{-4}$ rad
- Measurement of very small distance like size of molecule uses, Optical microscope, Electronic microscope and Tunneling microscope
- $1 \text{ AU} = 1.496 \times 10^{11} \text{ m}$
- $1 \text{ ly} = 9.46 \times 10^{15} \text{ m}$
- $1 \text{ parsec} = 3.08 \times 10^{16} \text{ m}$
- Size of proton 10^{-15} m
- Radius of Earth 10^7 m
- Distance to boundary 10^{26} m of observable universe

Measurement of mass

- SI unit is kilogram (kg)
- Unified atomic mass unit (u). It is used to measure mass of atoms and molecules
- $1 \text{ u} = 1/12 \times \text{mass of one } ^{12}\text{C atom}$
- $1 \text{ u} = 1.66 \times 10^{-27} \text{ kg}$
- Electron mass 10^{-30} kg
- Earth mass 10^{25} kg
- Observable universe 10^{55} kg

Measurement of time

- Atomic standard of time: This is based on caesium clock, uncertainty gained overtime by caesium atomic clock is less than 1 part in 10^{13} (loss of 3 μs in one year)
- Time span of most unstable particle 10^{-24} s
- Travel time for light from nearest star 10^8 s
- Age of universe 10^{17} s

Significant figures

- Reliable digits plus first uncertain digit are known as significant digit.
- A choice of change of different units does not change number of significant digits.
- All non-zero digits are significant.
- All zero between two non-zero digits are significant.
- The terminal zeros in a number without a decimal point are not significant.
- The trailing zeros in a number with decimal point are significant.

Rules of Arithmetic Operations with Significant Figures

- Addition/Subtraction: Final result contains as many decimal places as in number with least decimal places. e.g. $3.307 + 0.52 = 3.83$
- Multiplication/Division: Result contains as many significant figures as in number with least number of significant figures. e.g. $4.11/1.2 = 3.4$

Rounding off

- Preceding digit is raised by 1 if insignificant digit to be dropped is more than 5 and left unchanged of latter is less than 5.
- If insignificant digit is 5 then preceding digit is left unchanged if it's even and increased by 1 if it's odd.

SI system of units
(international system of units)

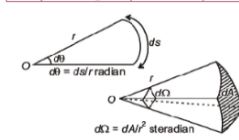
- Presently accepted internationally for measurement is SI system of units, revised in 2018. Certain rules to follow with standard symbols
- It is decimal system thus, conversion within system is easy and convenient
- It has 7 base unit and 2 supplementary units

Base Units

S.N.	Quantity	Unit	Symbol
1.	Length	meter	m
2.	Mass	kilogram	kg
3.	Time	second	s
4.	Electric current	ampere	A
5.	Thermodynamic temperature	kelvin	K
6.	Amount of substance	mole	mol
7.	Luminous intensity	candela	cd

Supplementary Units

S.N.	Quantity	Unit	Symbol
1.	Plane angle	radian	rad
2.	Solid angle	steradian	sr



Units and Measurements

Dimensional formulae and SI units of various physical quantities

S.N.	Physical Quantity	Base Units Relation with other quantities	Dimensional Formula	SI Unit
1.	Gravitational constant 'G'	$\frac{\text{Force} \times (\text{distance})^2}{\text{Mass} \times \text{mass}}$	$\frac{[MLT^{-2}][L^2]}{M \times M} = [M^{-1}L^3T^{-2}]$	$N m^2 kg^{-2}$
2.	Stress	$\frac{\text{Force}}{\text{Area}}$	$\frac{[MLT^{-2}]}{L^2} = [M^{-1}T^{-2}]$	$N m^{-2}$
3.	Coefficient of elasticity	$\frac{\text{Stress}}{\text{Strain}}$	$\frac{[ML^{-1}T^{-2}]}{1} = [ML^{-1}T^{-2}]$	$N m^{-2}$
4.	Surface tension	$\frac{\text{Force}}{\text{Length}}$	$\frac{[MLT^{-2}]}{L} = ML^{-1}T^{-2} = [ML^0T^{-2}]$	$N m^{-1}$
5.	Coefficient of viscosity	$\frac{\text{Force} \times \text{distance}}{\text{Area} \times \text{velocity}}$	$\frac{MLT^{-2} \times L}{L^2 \times LT^{-1}} = [ML^{-1}T^{-1}]$	$N m^{-2}$ or $Pa s$ or $decapoise$
6.	Planck's constant 'h'	$\frac{E}{\nu} = \frac{\text{Energy}}{\text{Frequency}}$	$\frac{ML^2T^{-2}}{T^{-1}} = [ML^2T^{-1}]$	J s
7.	Velocity gradient	$\frac{\text{Velocity}}{\text{Distance}}$	$\frac{LT^{-1}}{L} = T^{-1} = [M^0L^0T^{-1}]$	s^{-1}
8.	Pressure gradient	$\frac{\text{Pressure}}{\text{Distance}}$	$\frac{ML^{-1}T^{-2}}{L} = [ML^{-2}T^{-2}]$	$Pa m^{-1}$

Dimensional analysis

Dimensions

- Nature of physical quantity is determined by its dimension.
- The dimensions of physical quantity are powers to which base quantities are raised to represent it.
- The dimension of time in speed is -1

Dimensional equation

- The expression which shows how and which of the base quantities represent the dimension of physical quantity is called dimensional formula.
- An equation is obtained by equating physical quantity with its dimensional formula.
- For example $[A] = [M^0L^2T^0]$

Homogeneity principle

Physical quantities represented by symbols on both sides of a mathematical equation must have same dimensions.

Applications

Checking dimensional consistency of equations

- It is based on homogeneity law. An equation is dimensionally correct if dimension of fundamental quantities of each term on left side of equation is equal to that on right hand side.

Deducing relations among physical quantities.

- We should know the dependence of physical quantity on other upto three physical quantities and product type of dependence

Limitations of Dimensional Analysis

- Dimensional analysis is useful in deducing relations among inter dependent physical quantities but dimensional constant can not be determined.
- It can test dimensional validity but not exact relationship between physical quantities having same dimensions.
- It does not distinguish between the physical quantities having same dimensions.

Errors in measurement

Errors

Systematic

Random

Instrumental

Experimental

Personal

- Every measurement is approximate due to errors.
- Random errors occurs irregularly.
- Least count error is smallest value that can be measured by instrument (occurs within both systematic and random errors).

$$\text{Absolute error} = \frac{\sum (a_i - a_{mean})}{n}$$

$$\text{Relative error} = \frac{\Delta a_{mean}}{a_{mean}}$$

$$\text{Percentage error} = \frac{\Delta a_{mean}}{a_{mean}} \times 100$$

$$\text{If } X = \frac{A^a B^b}{C^c} \text{ Then } \% \frac{\Delta x}{x} = a \left(\% \frac{\Delta A}{A} \right) + b \left(\% \frac{\Delta B}{B} \right) + c \left(\% \frac{\Delta C}{C} \right)$$

Combination of errors

Sum and difference

$$\Delta Z = \Delta A + \Delta B$$

$$\frac{\Delta Z}{Z} = \frac{\Delta A}{A} + \frac{\Delta B}{B}$$

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